



## Can The Invisible Hand Draw The Railroad Timetable?

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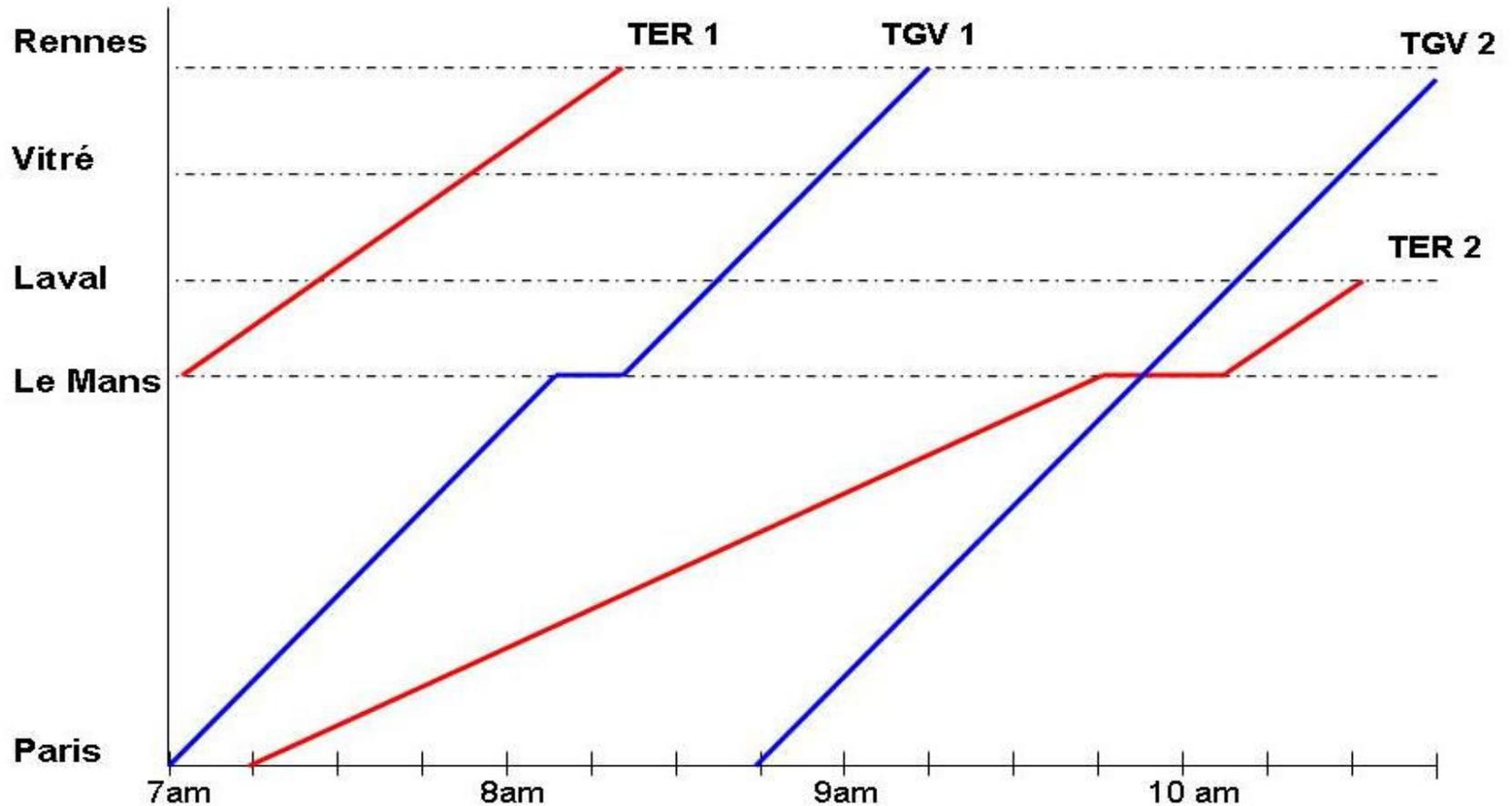
## Introduction (1/2)

- The railroad industry is currently being liberalized in Europe under the influence of the European Commission
- Goal of this process: to reduce costs and prices in the industry, trains can re-earn market shares over trucks, airplanes, personal cars, etc.
- This liberalization has lead to a separation between infrastructure and operations

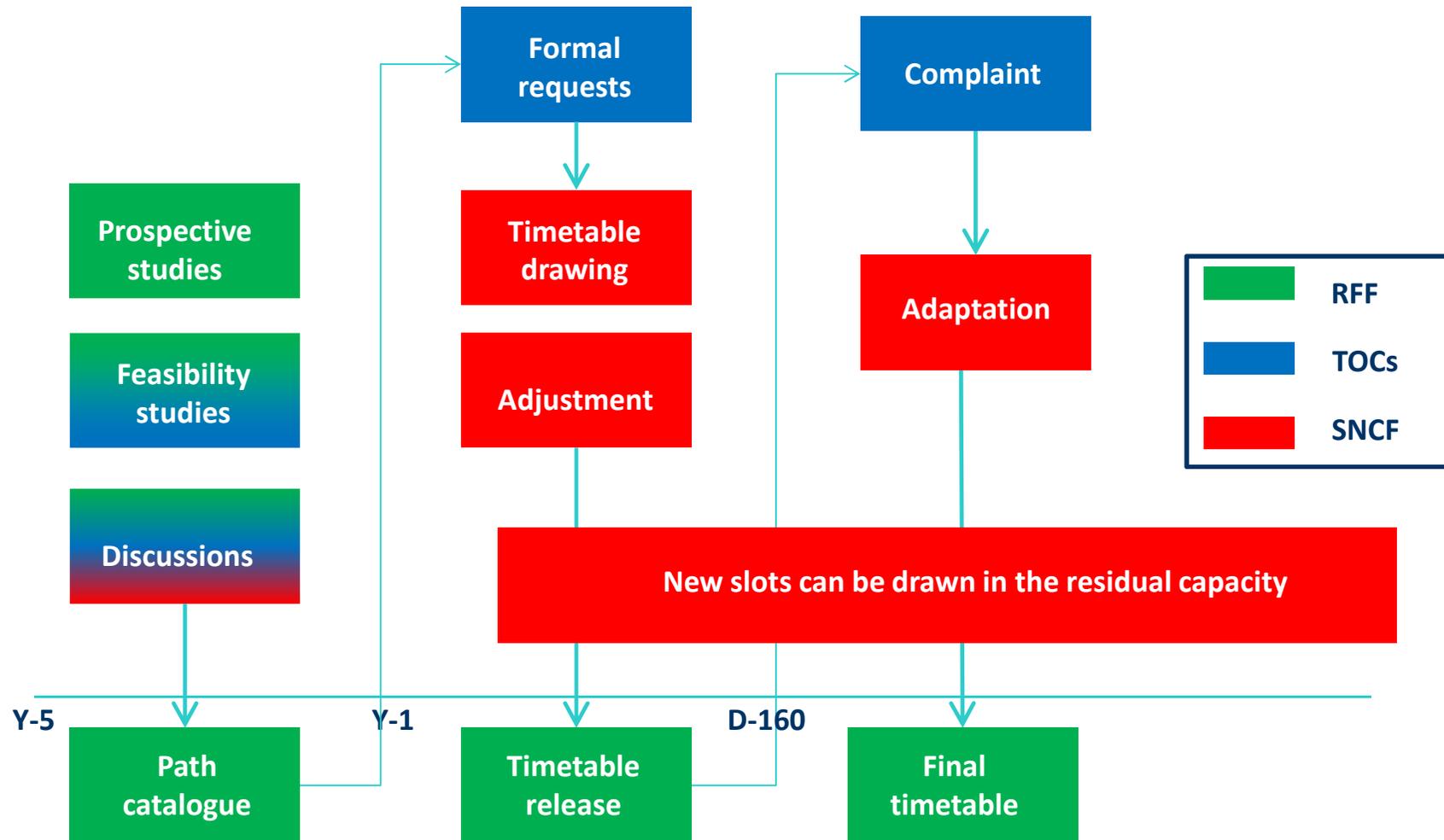
## Introduction (2/2)

- This article focuses on capacity allocation
- Liberalization and vertical separation will lead to a potential increase of demand for rail capacity.  
Currently:
  - the former vertically integrated incumbent does not ask for all the capacity it can use
  - Very few competitors, mostly on freight
- Capacity is hard to increase in the short term
- Solution: allocate capacity by market mechanisms?

# What is “capacity” in the railroad? industry



# An example of allocation process



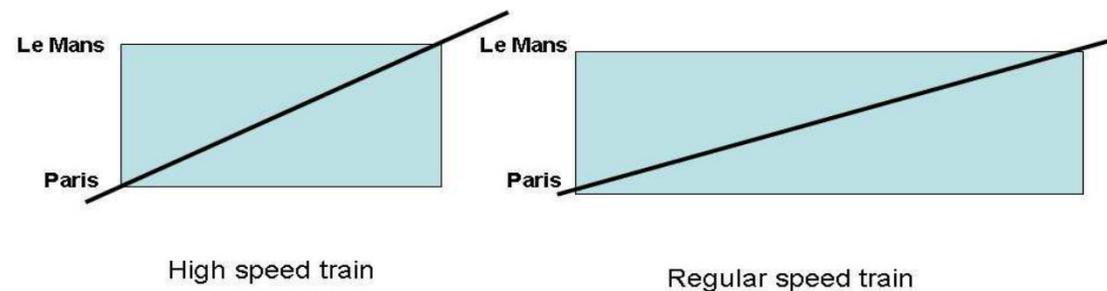
+ Prices are administratively set

## Specificities of rail capacities (1/2)

- Two key features:
  - a) The value of one train path is contingent to the overall pattern of service
  - b) slots are not homogenous goods and have an exclusionary property
- Property a) → slots may be substitutes OR complements → require to use combinatorial auctions
- Property b) → to fully optimize its capacity, the IM has to subdivide slots

## Specificities of rail capacities (2/2)

- To optimize the revenue of its network, the IM has to maximize the revenue of each block it sells.



- Formally:

$$\max \sum_{i \in I} \sum_{a \in A_H} p_a^i x_a^i$$

$$s.t. \sum_{a \in A_H} x_a^i \leq 1 \quad \text{and} \quad x_a^i \in \{0,1\}$$

→ NP hard problem

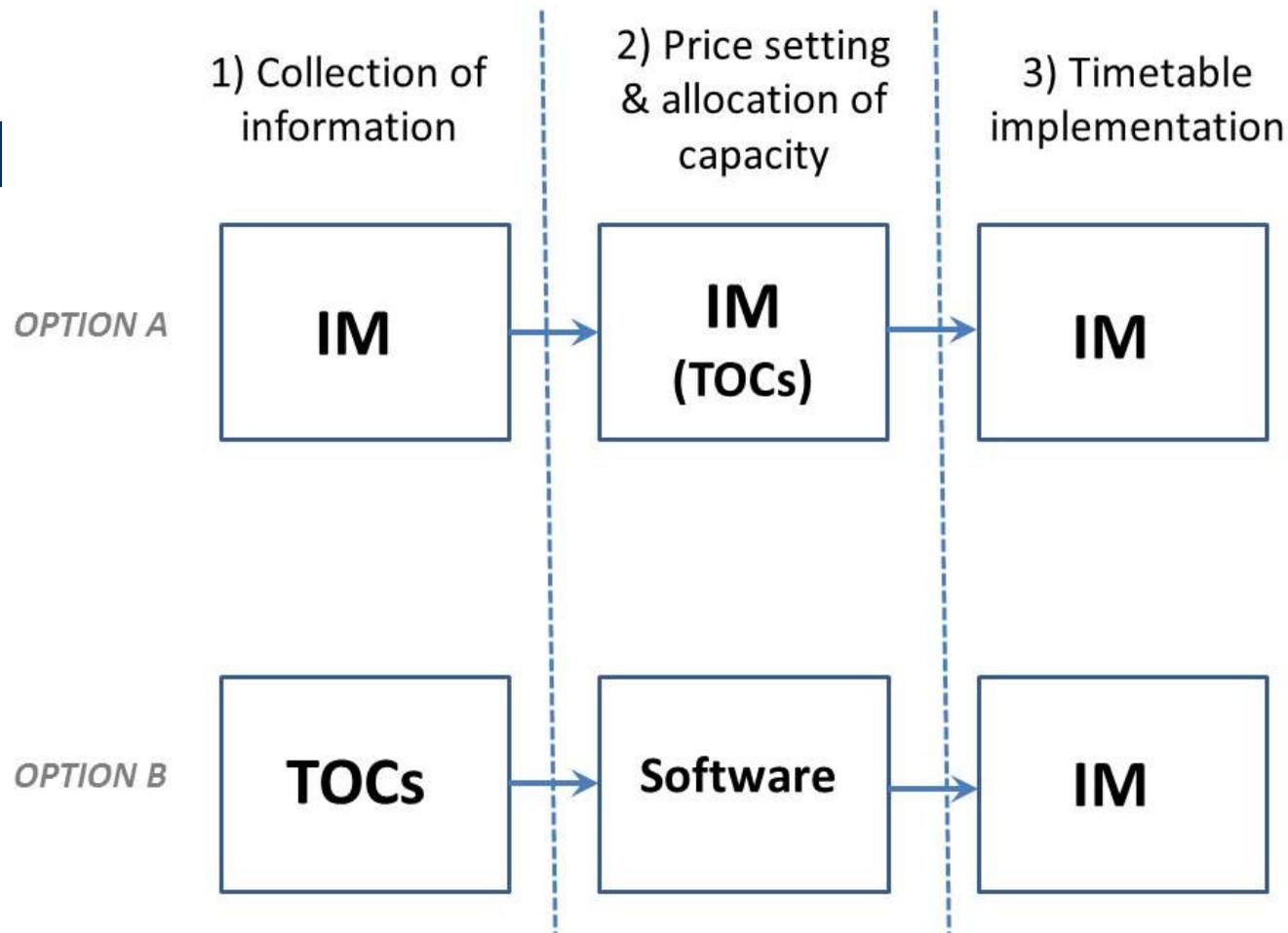
# Literature insight : rail literature

- Inspired by the liberalization process taking place in Sweden
- Coopers and Lybrand (1993): auctions are impossible because of the properties of rail capacity
- Brewer and Plott (1996): combinatorial auctions are possible (testbed environment)
- More complex network and techniques: Nilsson (2002), Borndörfer (2005), etc.
- But still some oppositions: Gibson (2003), Quinet (2003)

## Literature insight : CA literature

- Combinatorial auctions (CA) are doomed by early literature to be impossible to manage (winner determination is not trivial)
- Mid-1990s: CA are concretely used by the FCC to sale radio frequency
- New auctions designs to reduce the information burden to allow manageability (Rothkopf et al. 1998)
- **Nisan and Segal (2006) Blumrosen and Nisan (2010): to optimally sell  $n$  goods, one needs to know the price of the  $2^n - 1$  possible bundles. To allow a good approximation, the information burden still grows exponentially.**

# Two ways to allocate capacity



Most efficient way?

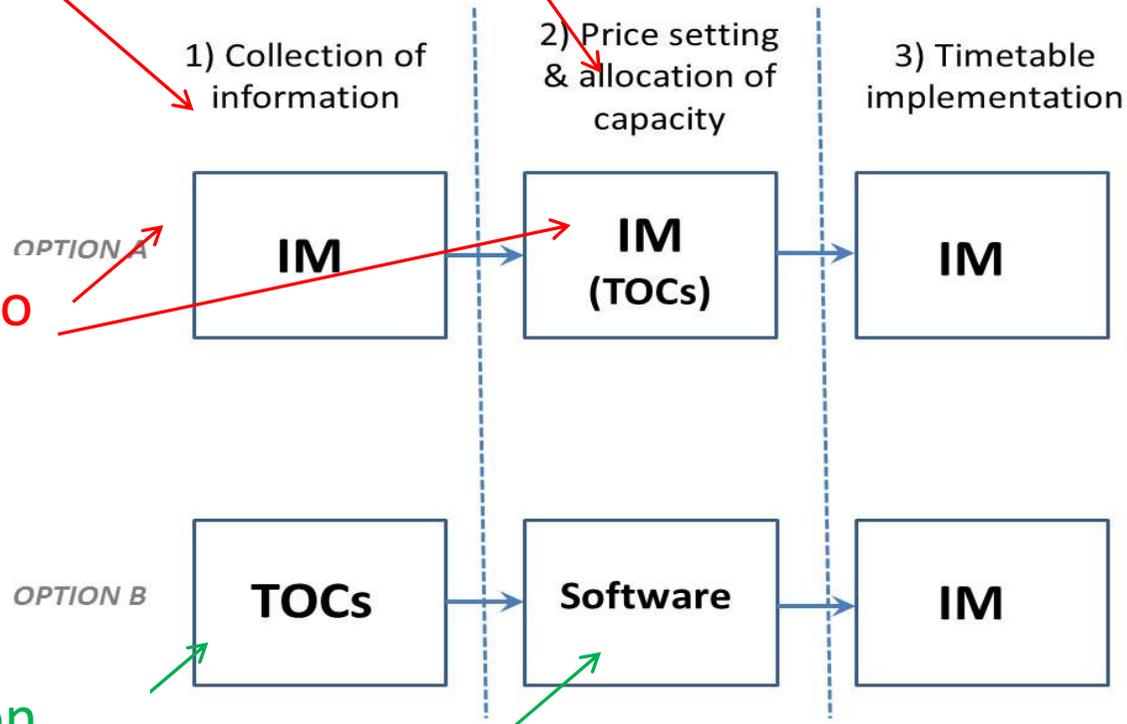
# Efficiency

No direct access to TOCs real valuation

No access to exact final demand

No incitation to be efficient

Competition lead to efficiency



Price depends on TOCs bids

# Transaction costs

- Costs in option A

$$C_{A,1}(M_i, I) = aI + \sum_{i \in I} b_i M_i$$

$$C_{A,2}(I, X, n) = eI + fX + gn$$

- Costs in option B

$$C_{B,1}(n) = \alpha(2^n - 1)$$

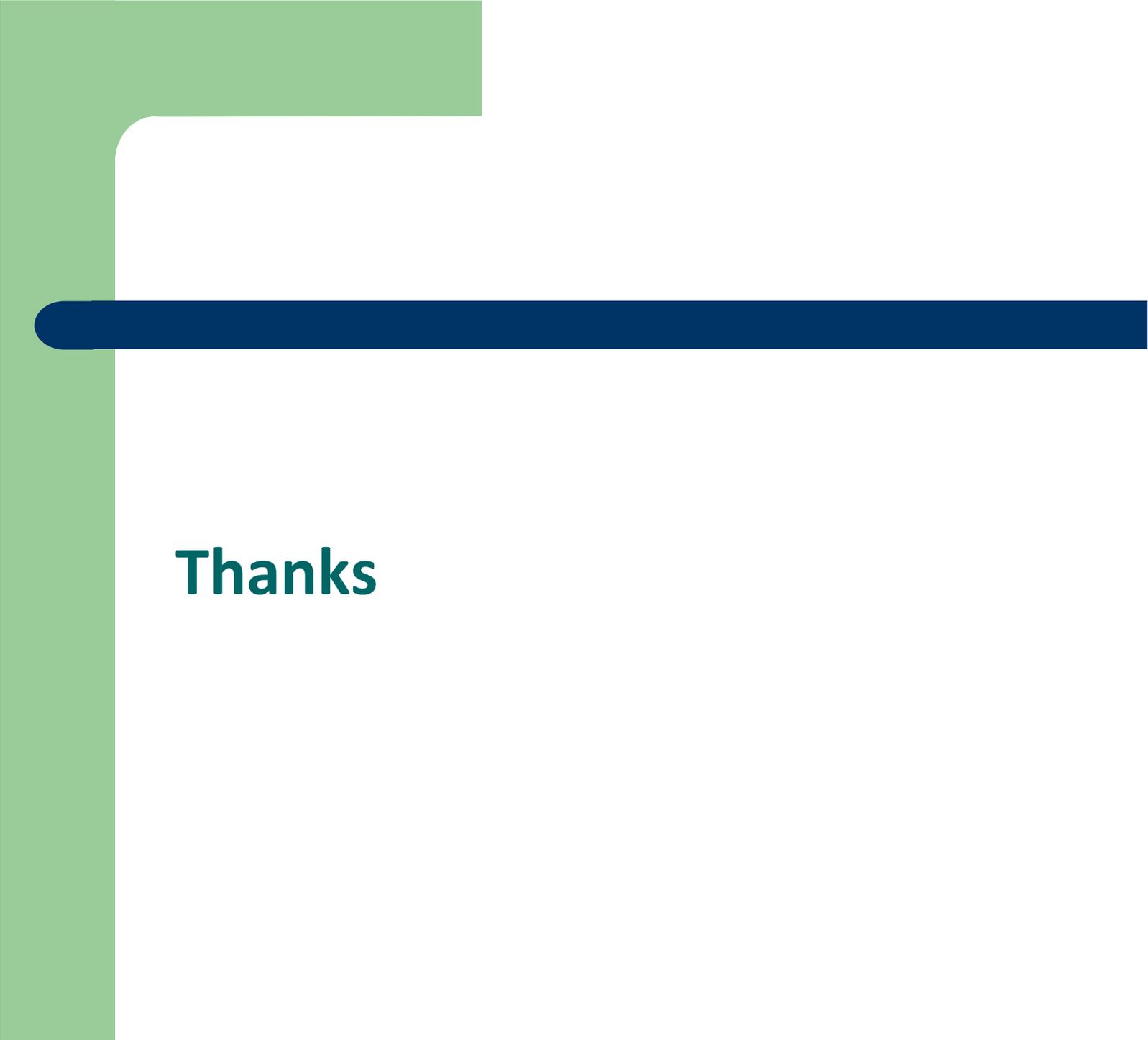
$$C_{B,2}(X, R) = \beta X + \gamma R$$

I: numbers of market,  $M_i$ : Size of market  $i$ , X: Complexity, n: number of slots, R:  
Numbers of rounds

- Exponential vs. linear evolution

# Conclusions

- Are auctions impossible to use to sell railroad capacity? NO
- Keep in mind manageability: a centralized entity draw the graph, but some of the slots can be auctions
- **The invisible hand cannot draw the (entire) timetable**
- Consequences for the current liberalization?
  - Competition for/on the network
  - Organization of information transparency?



**Thanks**